| Achievement Objectives | Number: Levels 4 and 5 | E |
| :---: | :---: | :---: |
|  | Level 4 <br> Number strategies and knowledge $\mathrm{AO2}$ : | CA |
|  | Understand addition and subtraction of fractions, decimals, and integers. |  |
|  | Number strategies and knowledge AO3: | $A C$ |
|  | Find fractions, decimals, and percentages of amounts expressed as whole numbers, simple fractions, and decimals Number strategies and knowledge AO4 |  |
|  | Apply simple linear proportions, including ordering fractions. | EA |
|  | Number strategies and knowledge AO5 |  |
|  | Know the equivalent decimal and percentage forms for everyday fractions. Number strategies and knowledge AO6 | AA |
|  | Know the relative size and place value structure of positive and negative integers and decimals to three places. Level 5 | AM |
|  | Number strategies and knowledge AO3: Understand operations on fractions, decimals, percentages, and integers. | AP |


| Strategies being developed | Problem progression | References | Knowledge being developed | Resources |
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| Find equivalent fractions by splitting, e.g. $\frac{3}{4}=\frac{15}{20}$, by splitting each quarter into fifths. | What would the part be called, if you cut...? <br> One third into 4 pieces $\left(\frac{1}{4} \times \frac{1}{3}=\frac{1}{12}\right)$ <br> One fifth into 3 pieces One sixth into 2 pieces One half into 6 pieces $\begin{aligned} & \frac{1}{4}=\overline{16}, \frac{1}{6}=\overline{36}, \frac{3}{4}=\overline{20}, \\ & \frac{3}{5}=9, \frac{7}{8}=\underline{28}, \\ & \frac{9}{10}=\overline{1000}, \end{aligned}$ | Teaching Fractions, Decimals and Percentages (Book 7) <br> Introduction (35-37) <br> Teaching Number Sense and Algebraic Thinking (Book 8) Equivalent Fractions (16) <br> Figure It Out <br> N3.1 Fun with Fractions (9) <br> N3.1 More Fractions (10) <br> N3.1 Racing to New Heights (14) <br> N3.3 Fraction Frenzy (22) <br> N3-4.1 A Watery Mission (3) <br> N3-4.2 (11) Sandwich Survey <br> NS\&AT 3.1 Fraction Tagging (18) <br> N7/8 L2 Boxed Biscuits (24) <br> PR 3-4.1 Paper Partitions (6) | Order decimals to three places, for examples, 6.25 and 6.3 | Teaching Number Knowledge <br> (Book 4) <br> Number Fans (4) <br> Place Value Houses (5) <br> More Reading of Decimal <br> Fractions (9) <br> Who Wins? (21) <br> Figure It Out <br> N 3 Decimal Day (15) <br> N 3.2 Jumping Along (20) <br> N 7/8 L. 2 Expanding With <br> Decimals (17) <br> N 7/8 4.3 Awesome Athletes (13) <br> N 7/8 4.5 Give it a Heave! (3) <br> N 7/8 4.5 Gentle Giants (18) |


| Strategies being developed | Problem progression | References | Knowledge being developed | Resources | CA |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Order fractions using equivalence and benchmarks, e.g. $\frac{2}{5}<\frac{7}{16}$ because $\frac{2}{5}$ is $\frac{1}{10}$ less than $\frac{1}{2}$ and $\frac{7}{16}$ is $\frac{1}{16}$ less. | Which fraction is bigger and by how much? $\begin{aligned} & \frac{3}{4} \text { or } \frac{2}{3}\left(\frac{1}{12}\right), \frac{4}{5} \text { or } \frac{3}{4}\left(\frac{1}{20}\right) \text {, } \\ & \frac{5}{8} \text { or } \frac{2}{3}\left(\frac{1}{24}\right), \frac{5}{8} \text { or } \frac{7}{12}\left(\frac{1}{24}\right), \\ & \frac{3}{8} \text { or } \frac{4}{10}\left(\frac{1}{40}\right), \frac{5}{6} \text { or } \frac{3}{4}\left(\frac{1}{12}\right) \text {, } \\ & \frac{17}{12} \text { or } \frac{5}{4}\left(\frac{1}{6}\right), \frac{7}{3} \text { or } \frac{11}{5}\left(\frac{2}{15}\right) . \end{aligned}$ | Teaching Number Sense and Algebraic Thinking (Book 8) <br> Estimating with Fractions (15) <br> Fractions (16) <br> Figure It Out <br> NS\&AT 3-4.1 Close Ties (14) | Order fractions, including halves, quarters, thirds, fifths, and tenths | Teaching Number Knowledge (Book 4) <br> Creating Fractions (6) <br> More Geoboard Fractions (7) <br> Non-unit Fractions (7) <br> Packets of Lollies (8) <br> Reading Decimal Fractions (8) <br> Card Ordering (12) <br> Arrow Cards (13) <br> Rocket - Where Will I Fit (15) <br> Who Has More Cake? (18) <br> Who Gets More? (20) <br> Bead Strings (17) <br> Figure It Out <br> N 2-3 Circle Segment (17) <br> N 2-3 Fabulous Folding (18) <br> N 2-3 How Many? (20) | $\begin{aligned} & A C \\ & \hline E A \\ & \hline A M \\ & \hline A P \end{aligned}$ |
| Find fractions of lengths, areas, volumes and other continuous quantities using reunitising, <br> e.g. three quarters of one half is three eighths | $\begin{aligned} & \frac{1}{2} \text { of } \frac{1}{2} \text { of } \frac{1}{2}=\frac{1}{8} \\ & \frac{2}{3} \text { of } \frac{1}{2}=\frac{2}{6}=\frac{1}{3} \\ & \frac{3}{4} \text { of } \frac{2}{3}=\frac{6}{12}=\frac{1}{2} \\ & \frac{3}{4} \text { of } \frac{3}{4}=\frac{9}{16} \\ & \frac{4}{5} \text { of } \frac{1}{3}=\frac{4}{15} \\ & \hline \end{aligned}$ | Figure It Out <br> PR 3+ Puzzling Patterns (1) <br> PR 3+ Shaping Up (2) <br> PR 3+ What Do You See? (6) <br> PR 3-4.1 Tri Fractions (4) | Record the results of mental calculations using equations and diagrams, for example, empty number line |  |  |


| Transition: Advanced Additive to Advanced Multiplicative |  |  | Domain: Ratios and Proportions |  |
| :---: | :---: | :---: | :---: | :---: |
| Strategies being developed | Problem progression | References | Knowledge being developed | Resources |
| Find fractions of whole number amounts using multiplication and division, <br> e.g. $\frac{2}{3}$ of $36=\square$ $\left(\frac{2}{3} \times 36\right)$. | $\frac{3}{5}$ of $60=\square, \frac{5}{8}$ of $64=\square$, $\frac{5}{6}$ of $42=\square, \frac{4}{7}$ of $56=\square$ $\frac{3}{5}$ of $\square=27, \frac{4}{9}$ of $\square=16$, $\frac{7}{10}$ of $\square=84$, $\frac{8}{8}$ of $72=27$, $\frac{12}{12}$ of $48=28$ | Teaching Number Sense and Algebraic Thinking (Book 8) Whole Numbers Times Fractions (22) Fractions Times Whole Numbers (23) <br> Figure It Out <br> N3.2 Heading for Home (24) <br> N3.3 Marble Marvels (21) <br> N3-4.2 Funky Fractions (12) <br> N3-4.2 Measuring Up (13) <br> N3-4.3 Sporting Fractions (16) <br> NS \& AT 3.2 On Top of the World (22) <br> NS7/8 4.2 Mystery Fractions (21) <br> N7/8 L2 Placing Points (18) <br> N7/8 4.3 Linking Lollies (1) <br> N7/8 4.3 Football Fractions (4) <br> PR 3+ Star Clusters (5) <br> PR 3-4.1 Fraction Extraction (8) | Recall fraction $\Leftrightarrow$ decimal $\Leftrightarrow$ percentage conversions for halves, thirds, quarters, fifths, and tenths | Teaching Number Knowledge (Book 4) <br> Equivalent Fractions, Decimals <br> and Percentages (21) <br> Bead Strings (17) <br> Figure It Out <br> N3.1 (13) Friendly Fractions <br> N 3-4 (11) A Long Look at Decimals <br> N 3-4.2 (15) Fraction Distraction <br> N 3-4.3 (24) Hidden Help <br> BF 3-4 (21) Mystery Decimals <br> BF 3-4 (24) Decimal Spotting <br> N 7/8 L2 (9) Seeing Double <br> N 7/8 L2 (20) Getting the Point |
| Multiply fractions by other fractions, e.g. $\frac{2}{3} \times \frac{3}{4}=\frac{6}{12}=\frac{1}{2}$ | $\begin{aligned} & \frac{1}{2} \times \frac{3}{4}=\frac{3}{8}, \frac{2}{3} 3 \frac{3}{5}=\frac{6}{15}=\frac{2}{5}, \\ & \frac{3}{4} \times \frac{2}{5}=\frac{6}{20}, \frac{5}{8} \times \frac{1}{2}=\frac{5}{5}, \\ & \frac{2}{3} \times \frac{1}{5}=\frac{2}{15}, \frac{5}{6}, \frac{2}{3}=\frac{10}{18}=\frac{5}{9}= \end{aligned}$ | Teaching Number Sense and Algebraic Thinking (Book 8) A Fraction Times a Fraction (24) When Big Gets Smaller (24) |  |  |

## Transition: Advanced Additive to Advanced Multiplicative

| Strategies being developed | Problem progression | References | Knowledge being developed | Resources |
| :---: | :---: | :---: | :---: | :---: |
| Rename improper fractions as mixed numbers using division, and position improper fractions on a number line. | $\begin{aligned} & \frac{27}{4}=6 \frac{3}{4}, \frac{43}{5}=8 \frac{3}{5}, \\ & \frac{23}{3}=7 \frac{2}{3}, \frac{65}{9}=7 \frac{2}{9}, \\ & \frac{76}{8}=9 \frac{1}{2}, \frac{100}{3}=33 \frac{1}{3} \end{aligned}$ | Teaching Number Sense and Algebraic Thinking (Book 8) Fractions Greater Than 1 (17) <br> Figure It Out <br> PR 3-4.1 Fraction Line-up (2) | Recall equivalent fractions for halves, thirds, quarters, fifths, and tenths with numbers to 100 and with 1000 | Teaching Number Knowledge (Book 4) Super Liquorice (19) <br> Little Halves and Big Quarters (19) <br> Equivalent Fractions, Decimals and <br> Percentages (21) <br> The Same But Different (30) <br> Figure It Out <br> N 3.1 Fun With Fractions (9) <br> N 3.1 More Fractions (10) <br> N 3.1 To Market, To Market (11) <br> N 3.3 Fraction Frenzy (22) <br> N3-4.2 Sandwich Survey (11) <br> N 7/8 L. 1 Chocolate Chip Feast (22) <br> N 7/8 L. 2 Classy Courtyards (22) <br> PR 3-4.2 The Equivalence Game (18) |

Domain: Ratios and Proportions

| Transition: Advance | Additive to Adva | Multiplicative Dom | Domain: |  | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Strategies being developed | Problem progression | References | Knowledge being developed | Resources | CA |
| Solve division problems that have fraction answers, e.g. 8 $\div 3=2 \frac{2}{3}$, and connect division with the numerator and denominator of the answer, e.g. $4 \div 5=\frac{4}{5}$. | $\begin{aligned} & 5 \div 4=\square, 8 \div 3=\square, \\ & 12 \div 5=\square, 5 \div 6=\square, \\ & 3 \div 7=\square, 13 \div 8=\square, \\ & 1 \div \square=\frac{1}{7}, 7 \div \square=2 \frac{1}{3}, \\ & 2 \div \square=\frac{2}{5}, 17 \div \square=1 \frac{7}{10}, \\ & \square \div 3=3 \frac{1}{3}, \square \div 5=1 \frac{4}{5}, \\ & \square \div 6=1 \frac{5}{6}, \square \div 9=4 \frac{8}{9}, \end{aligned}$ | Figure It Out <br> N3.1 Friendly Fractions (13) <br> N 7/8 4.5 Revisiting Remainders (1) | Round whole numbers and decimals with up to two places to the nearest whole number or tenth | Teaching Number <br> Knowledge (Book 4) <br> Sensible Rounding (28) <br> Swedish Rounding (28) <br> Figure It Out <br> N 3-4 . 3 Paddle On (6) <br> N 7/8 4.5 Body Mass (10) | EA <br> AA <br> AM |
| Convert fractions to decimals, and percentages and vice versa. | $\begin{aligned} & 3 \div 2=1 \frac{1}{2}=1.5=150 \% \\ & 5 \div 4=1 \frac{1}{4}=1.25=125 \% \\ & 3 \div 8=\frac{3}{8}=0.375=37.5 \% \\ & 2 \div 3=\frac{2}{3}=0.6=66.6 \% \\ & \frac{7}{5}=\square, \frac{5}{7}=\square . \end{aligned}$ | Teaching Fractions, Decimals and Percentages (Book 7) <br> Deci-mats (41-44) <br> Figure It Out <br> BF 3-4 Mystery Decimals (21) <br> BF 3-4 Decimal Spotting (24) <br> N 3-4.1 Waves Win (8) <br> N 3-4.1 Bottle Up (10) <br> N 3-4.1 A Long Look at Decimals (11) <br> NS 7/8 4.2 Pizza Pieces (19) <br> N 7/8 L2 Seeing Double (9) <br> N 7/8 L2 Getting the Point (20) <br> N 7/8 4.3 Conversion Cousins (2) <br> PR 3+ Discount Deals (8) |  |  | AP |

Transition: Advanced Additive to Advanced Multiplicative
Domain: Ratios and Proportions

| Strategies being developed | Problem progression | References |
| :---: | :---: | :---: |
| Estimate and find percentages of whole number amounts using benchmark percentages, <br> e.g. $65 \%$ of $\$ 80$ as $50 \%$ is $\$ 40,10 \%$ is $\$ 8,5 \%$ is $\$ 4$, so $\$ 40+\$ 8+\$ 4=\$ 52$ | ```\(10 \%\) of 48 so \(30 \%\) of 48 \(50 \%\) of 64 so \(25 \%\) of 64 \(10 \%\) of 28 so \(5 \%\) of 28 \(50 \%\) of \(56,10 \%\) of 56 so \(60 \%\) of 56 \(10 \%\) of \(35,5 \%\) of 35 so \(15 \%\) of 35 \(50 \%\) of \(140,10 \%\) of \(140,5 \%\) of 140 so \(65 \%\) of 140``` | Teaching Fractions, Decimals and Percentages (Book 7) Hot Shots (47-49) <br> Figure It Out <br> NS \& AT 3-4.1 Pondering Percentages (12) <br> N3.2 Better Buy Bargains (18) <br> N 3.3 Surf's Up (24) <br> N 3-4.1 Hot Shots (12) <br> N 3-4.2 Making Money (16) <br> NS\&AT 3-4.1 Pondering Percentages (12) <br> NS 7/8.L1 Playzone Discount (16) <br> NS 7/8 4.2 People Power (15) <br> N 7/8 4.3 Involving Interest (6) <br> N 7/8 4.3 New Car Capers (14) <br> N 7/8 4.5 Bargain Bonanza (14) <br> N 7/8 4.6 Spending on Sport (10) <br> PR 3+ Getting Tough (14) |
| Add and subtract fractions with related denominators, e.g. $\frac{3}{4}+\frac{5}{12}=\frac{14}{12}=1 \frac{2}{12}$. | $\begin{aligned} & \frac{3}{4}+\frac{3}{4}=\frac{6}{4}=1 \frac{1}{2} \\ & \frac{2}{3}+\frac{4}{3}=\frac{6}{3}=2 \\ & \frac{4}{5}-\frac{2}{5}=\frac{2}{5} \\ & \frac{3}{4}+\frac{5}{8}=\frac{11}{8}=1 \frac{3}{8} \\ & \frac{9}{10}-\frac{3}{5}=\frac{3}{10} \\ & \frac{2}{3}+\frac{5}{6}=\frac{9}{6}=1 \frac{1}{2} \\ & \frac{7}{8}-\frac{1}{2}=\frac{3}{8} \end{aligned}$ | Teaching Fractions, Decimals and Percentages (Book 7) Comparing Apples with Apples (38) <br> Teaching Number Sense and Algebraic Thinking (Book 8) <br> Estimating with Fractions (15) <br> Figure It Out <br> N 3.3 Stacking Up (20) <br> N 7/8 4.5 Egyptian Fractions (23) <br> PR 3-4.1 Galloping Greyhounds (1) |

NS\&AT 3-4.1 Pondering Percentages (12)

N 7/8 43 Involving Interest (6)
N 7/84.3 New Car Capers (14)
N 7/8 4.5 Bargain Bonanza (14)

Teaching Fractions, Decimals and Percentages (Book 7)
Comparing Apples with Apples (38)

Teaching Number Sense and Algebraic Thinking (Book 8)
Estimating with Fractions (15)

## Figure It Out

解 Up (20)

PR 3-4.1 Galloping Greyhounds (1)

Transition: Advanced Additive to Advanced Multiplicative
Domain: Ratios and Proportions

| Strategies being developed | Problem progression | References |
| :---: | :---: | :---: |
| Add and subtract decimals. | $\begin{array}{\|l\|} \hline 1.2+3.8=4 \\ 0.75+1.25=2 \\ 5-2.25=2.75 \\ 0.5+1.25=1.75 \\ 2.5-1.75=0.75 \\ 0.375+1.625=2 \\ 3-0.001=2.999 \\ 2.673+1.327=4 \\ 5.2-1.68=3.52 \end{array}$ | Teaching Fractions, Decimals and Percentages (Book 7) <br> Pipe Music with Decimals (38-41) <br> How Can Two Decimals so Ugly..? (45-46) <br> Figure It Out <br> N 3.2 Target Time (16) <br> N 3.2 Dallying with Decimals (17) <br> N 3-4.3 Riding the Waves (2) <br> N 7/84.3 Going for Gold! (12) <br> Pr 3+ Make 1.5 (18) |
| Solve measurement problems with related fractions, by recognising equivalent fractions, e.g. How many sixths are in one and one half? $\left(1 \frac{1}{2} \div \frac{1}{6}=\frac{9}{6} \div \frac{1}{6}=9\right)$ | Wholes and parts: e.g. cakes and pieces, lolly snakes and pieces, etc. <br> How many...? | Teaching Number sense and Algebraic Thinking (Book 8) Dividing Fractions (21) |

Transition: Advanced Additive to Advanced Multiplicative

| Strategies being developed | Problem progression | References |
| :---: | :---: | :---: |
| Show the order of decimal numbers by developing a number line scale | On a 0-5 scale show: 2.5, 1.25, 4.9, 3.75, 0.67 <br> On a 0-2 scale show: $0.2,1.8,0.66,1.95,1.125$ | Teaching Number sense and Algebraic Thinking (Book 8) <br> Scales on Number Lines (19) <br> Whole Number Rounding (19) <br> Confusing Fractions and Decimals (20) |
| Solve simple rate problems using multiplication, e.g. Picking 7 boxes of apples in $\frac{1}{2}$ hour is equivalent to 21 boxes in $1 \frac{1}{2}$ hours. | Washing cars: <br> 4 in 1 hour $=32$ in 8 hours <br> 7 in 2 hours $=35$ in 10 hours <br> 3 in $\frac{1}{2}$ hour $=18$ in 3 hours <br> 9 in $1 \frac{1}{2}$ hours $=36$ in 4 hours <br> 5 in $\frac{3}{4}$ hour $=40$ in 6 hours | Figure it Out <br> N 3.3 Numbers on the Line (2) <br> N 3-4.1 More Thinking (21) <br> N 3-4.2 Paddling Down the Waikato (19) <br> N 3-4.3 Challenge Time (4) <br> N 3-4.3 Paddle On (6) <br> N 3-4.3 Feel the Beat (11) <br> NS 7/8.1 Grocery Grapplers (20) <br> NS 7/8.1 Shopping Around (22) <br> N 7/8 4.3 Kapa Haka Hāngi (17) <br> PR 3+ Speed Read (10) <br> PR 3+ Demolition Dollars (16) <br> PR 3+ Painting by Numbers (17) <br> PR 3+ Tiring Teamwork (21) |
| Find equivalent ratios using multiplication and division and express them as equivalent fractions, e.g. $16: 8$ as $8: 4$ as $4: 2$ as $2: 1$ and $\frac{16}{24}=\frac{8}{12}=\frac{4}{6}=$ $\frac{2}{3}$ | $10: 15$ as $2: 3$ and $\frac{10}{25}=\frac{2}{5}$ $20: 10$ as $10: 5$ as $2: 1$ and $\frac{20}{30}=\frac{10}{15}=\frac{2}{3}$ $12: 36$ as $6: 18$ as $3: 9$ as $1: 3$ and $\frac{12}{18}=\frac{6}{18}$ $=\frac{3}{9}=\frac{1}{4}$ <br> $18: 27$ as $6: 9$ as $2: 3$ and $\frac{18}{45}=\frac{6}{15}=\frac{2}{5}$ <br> $45: 15$ as $9: 3$ as $3: 1$ and $\frac{45}{60}=\frac{9}{12}=\frac{3}{4}$ <br> $16: 48$ as $8: 24$ as $4: 12$ as $2: 6$ as $1: 3$ and $\frac{16}{64}=\frac{8}{32}=\frac{4}{16}=\frac{2}{8}=\frac{1}{4}$ | Teaching Fractions, Decimals and Percentages (Book 7) <br> Mixing Colours (50-52) <br> Figure it Out <br> N 3-4.1 Stretch and Grow (4) <br> N 3-4.1 Bean Brains (9) <br> NS\&AT 3.1 Run Like the Wind (12) <br> NS\&AT 3-4.2 Lunchtime Mardi Gras (18-20) <br> NS 7/8 4.2 Balancing Act (22) <br> N 7/8 4.5 Bargain Packs (15) <br> N 7/8 4.6 Hypertufa Tiles (17) <br> PR 3+ Chocolate Choices (4) <br> PR 3+ Pop Star Pics (20) <br> PR 3-4.1 Smart Sizes (21) <br> PR 3-4.1 The Right Gear (20) |

